# $3^{\text {rd }}$ Assignment (Apr. 2020) <br> Year 1440-1441 H $2^{\text {nd }}$ Semester 

| Course name \& code | 441 | اسم ورمز المقرر |
| :---: | :---: | :---: |
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## Instruction and guides for the assignment:

1. This assignment is designed to guide you to understand fully the topics and practice covered in the $1^{\text {st }}$ month of the course.
2. To give you plenty of time to review and apply the materials for the answer, the assignment duration is from 2:00pm Thursday April 16 until Saturday Apr. 18 @ 11:00 before midnight
3. You can use the lecture notes, the textbook, Excel for your answer.
4. You are the guardian of your behavior in this assignment. This assignment is totally for your independent effort. Do not attempt to collaboration or communication with anyone about the questions of the assignment, it is totally not allowed by any means.
5. Write all your answers on an Excel file. The file must contain both active work sheet and fixed worksheet. Put all the fixed answers in single worksheet and name it as (Fixed Ans.). Make sure to clearly indicate the number of the question answered.
6. Email you files to the address knowibet@ksu.edu.sa . Write the subject of the email as:

OPER-441-Assignment\#3 <<Section Number>> , << your name>> , <<your KSU ID >>
7. Make sure to make your document as organized as possible.

وفقكم الله ويسر لكم .. وحفظكم ورعاكم

## Application \#1:

ABC Department store sells modern style clothing. The cost per unit of the new style clothing is random following the distribution:

| Price (SR) | $\mathbf{5}$ | $\mathbf{6}$ | $\mathbf{7}$ | $\mathbf{8}$ | $\mathbf{9}$ | $\mathbf{1 0}$ | $\mathbf{1 1}$ | $\mathbf{1 2}$ | $\mathbf{1 3}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Prob. | 0.0168 | 0.0896 | 0.2090 | 0.2787 | 0.2322 | 0.1239 | 0.0413 | 0.0079 | 0.0007 |

Also, the selling price (per unit) is a random variable. The clothing style is seasonal. Meaning, if the style is sold during the season, then they will have a high value. If the clothing is sold out of season then the store must announce special offers to sell the leftovers. The special offer prices is considered random variable. Model this system using simulation under the following cases.

## Case-I

- The demand on the clothing is a random variable that follows the shifted Bionomial distribution with shift $\delta=100$ and parameters ( $n=50, p=0.6$ ).
- Selling price during the season follows discrete integer value between 10 and 20 and shifted by the unit cost. For example, if ABC store buy the unit for 12 SR, then the selling price is shifted discrete uniform with shift $\delta=12$.
- The leftover is sold at a fixed discount of $60 \%$ from the selling price. For example, if the selling price per unit is 25 SR during the season then the special offer price by the end of season is 10 SR .

ABC store wants to decide whether to order $\mathrm{Q}=100$ units, $\mathrm{Q}=150$ units or $\mathrm{Q}=200$ units for the next season. Using simulation on Excel, find the best decision using the net profit function of the demand and the order quantity. Perform the following:
a. Using data table (fixed data) for 500 simulation runs, give the average of net profits, standard deviation, $95 \%$ confidence interval.
b. Make a histogram for the simulation output in the data table using excel

## Case-II

- The demand on clothings is a random variable that follows the positive integer normal distribution with $\mu=120$ and $\sigma=20$ (use abs(int(...)) function in excel)
- Selling price during the season follows shifted Bionomial distribution with shift $\delta=$ unit cost and parameters ( $n=10, p=0.35$ ).
- The leftover is sold at a random discount follows discrete uniform $D U[40 \%, 65 \%]$ from the selling price.
ABC store wants to decide whether to order $\mathrm{Q}=80$ units, $\mathrm{Q}=120$ units or $\mathrm{Q}=160$ units for the next season. Using simulation on Excel, find the best decision using the net profit function of the demand and the order quantity. Perform the following:
a. Using data table (fixed data) for 500 simulation runs, give the average of net profits, standard deviation, $95 \%$ confidence interval.
b. Make a histogram for the simulation output in the data table using excel


## Application \#2:

Patients arrive to a dental clinic according to a random process. The patients are served as first come first served bases. If the patient arrive and find the dentist busy he waits for his turn. Assume that the waiting room is infinite. Simulate this application under the following cases.

## Case-I

- All patients request the same service which takes a random amount of time (in minutes) that follows integer exponential with mean $=15$ minutes and shift parameter $\delta=5$ minutes.( use integer function int(...))
- The time between arrivals is assumed to follow exponential with mean = 10 and shift parameter $\delta$ where $\delta \sim$ discrete uniform between 8 minutes and 15 minutes
a. Using simulation on Excel to evaluate the performance of the clinic by using data table (fixed data) for 100 simulation runs, each run has 100 arrivals and give the values of (i), (ii) and(iii), standard deviation and 95\% confidence interval.
i. The average waiting time for a patient if he wait.
ii. The percentage that there is no patients in the clinic.
iii. The average number of patients served per hour.

b. Using your simulation output for 100 arrival, fixed the data and find the distribution of number of patients in the system $N(t)$ for $N=0,1,2,3,4,5,6,7,8,9,10$ only.


## Case-II

- Patients request one of three same service which takes a random amount of time

| Service Type | Percentage Patients | Service time |
| :--- | :--- | :--- |
| Service 1 | $45 \%$ of the patients | Discrete uniform [10, 20] |
| Service 2 | $35 \%$ of the patients | integer exponential with mean = 15 minutes <br> and shift parameter $\delta=5$ (use int(..) ) |
| Service 3 | $20 \%$ 0f the patients | Integer Gamma dist. With $\alpha=5$ and $\beta=4$ |

- The time between arrivals is assumed to follow exponential with mean = 10 and shift parameter $\delta$ where $\delta \sim$ discrete uniform between 8 minutes and 15 minutes

Using simulation on Excel to evaluate the performance of the clinic by using data table (fixed data) for 100 simulation runs, each run has 100 arrivals and give the values of (i), (ii) and(iii), standard deviation and 95\% confidence interval.
i. The average waiting time for a patient if he wait.
ii. The percentage that there is no patients in the clinic.
iii. The average number of patients served per hour.

| Patient \# | Time between Patients | Arrival <br> Time | Service <br> Type | Service <br> Time | Starting service | Patient Wait?? | Waiting <br> Time | Dep Time | Clinic Idle Time |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |  |  |  |  |
| 2 |  |  |  |  |  |  |  |  |  |
| 3 |  |  |  |  |  |  |  |  |  |
| 4 |  |  |  |  |  |  |  |  |  |
| 5 |  |  |  |  |  |  |  |  |  |
| 6 |  |  |  |  |  |  |  |  |  |
| 7 |  |  |  |  |  |  |  |  |  |
| 8 |  |  |  |  |  |  |  |  |  |
| 9 |  |  |  |  |  |  |  |  |  |

## Application \#1:

Unit cost

| Price $(\mathrm{SR})$ | $\mathbf{5}$ | $\mathbf{6}$ | $\mathbf{7}$ | $\mathbf{8}$ | $\mathbf{9}$ | $\mathbf{1 0}$ | $\mathbf{1 1}$ | $\mathbf{1 2}$ | $\mathbf{1 3}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Prob. | 0.0168 | 0.0896 | 0.2090 | 0.2787 | 0.2322 | 0.1239 | 0.0413 | 0.0079 | 0.0006 |

## Case-I

- Demand: shifted Bionomial $(n=50, p=0.6)$ with shift $\delta=100$
- Selling Price: Discrete Integer (10 and 20) and shifted by the $\delta=$ unit cost.
- The Leftover Value: discount of $60 \%$ from the selling price.



Order quantities: $\mathrm{Q}=100$ units, $\mathrm{Q}=150$ units or $\mathrm{Q}=200$. Perform the following:
a. Data Table for 500 simulation runs: give the average of net profits, standard deviation, 95\% confidence interval.
b. Make a histogram for $\mathrm{G}(\mathrm{Q}, \mathrm{D})$ of the best Q only

| Q | 100 | 150 | 200 |
| :---: | :---: | :---: | :---: |
| Average | 1505.4 | 1947.73 | 2058.1 |
| STDV | 315.769 | 442.457 | 487.954 |
| LB-95\% | 1477.65 | 1908.85 | 2015.22 |
| UB-95\% | 1533.15 | 1986.6 | 2100.97 |

Q $100 \quad 150 \quad 200$

| averge | 1493.4 | 1961.208 | 2011.777 |
| :--- | :---: | :---: | :---: |
| STDEV | 317.5817 | 452.9802 | 485.1641 |
| LB-95\% | 1465.496 | 1921.407 | 1969.148 |
| UB-95\% | 1521.304 | 2001.009 | 2054.406 |

## Case-II

- Demand: positive integer normal distribution with $\mu=120$ and $\sigma=20$ (use abs(int(...)) function in excel)
- Selling Price: Bionomial $(n=10, p=0.35)$ with shift $\delta=$ unit cost.
- The Leftover Value: discount DU[40\%,65\%] from the selling price

| Q | $\mathbf{8 0}$ | $\mathbf{1 2 0}$ | $\mathbf{1 6 0}$ |
| :---: | :---: | :---: | :---: |
| Average | 276.601 | 379.302 | 320.221 |
| STDV | 116.885 | 191.297 | 259.569 |
| LB-95\% | 266.33 | 362.493 | 297.414 |
| UB-95\% | 286.871 | 396.11 | 343.028 |


|  | $\mathrm{q}=80$ | $\mathrm{q}=120$ | $\mathrm{q}=160$ |
| :---: | :---: | :---: | :---: |
| Average of net profit | 261.23 | 355.38 | 306.34 |
| standard diviation | 122.97 | 193.70 | 243.22 |
| LB- 95\% | 250.43 | 338.36 | 284.97 |
| UB- 95\% | 272.04 | 372.40 | 327.71 |


| Get Sxternal Data |  | Connections | Sort \& Filter |  | $\cdots$ | Data Tools |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |
| H1 | $v: \times \vee f_{x}$ |  |  |  |  |  |  |  |
| A |  | в | c | D | E | F | G | H |
| 1 | ABC Store |  |  |  |  |  |  |  |
| 2 | Case 2 |  |  |  |  |  |  |  |
| 3 |  |  |  |  |  |  |  |  |
| 4 |  |  |  | Vlookup Table |  |  |  |  |
| 5 | cost per unit | 7 |  | prob. | LB | CDF | Cost (SR) |  |
| 6 | Demand | 83 |  | 0.0168 | 0 | 0.0168 | 5 |  |
| 7 | Selling price | 8 |  | 0.0896 | 0.0168 | 0.1064 | 6 |  |
| 8 | leftover price | 3.36 |  | 0.209 | 0.1064 | 0.3154 | 7 |  |
| 9 |  |  |  | 0.2787 | 0.3154 | 0.5941 | 8 |  |
| 10 | Q | 120 |  | 0.2322 | 0.5941 | 0.8263 | 9 |  |
| 11 |  |  |  | 0.1239 | 0.8263 | 0.9502 | 10 |  |
| 12 | Total Slaes | 664 |  | 0.0413 | 0.9502 | 0.9915 | 11 |  |
| 13 | Left over vlaue | 124.32 |  | 0.0079 | 0.9915 | 0.9994 | 12 |  |
| 14 | Total production cost | 840 |  | 0.0007 | 0.9994 | 1 | 13 |  |
| 15 | Net profit |  |  |  |  |  |  |  |
| 16 |  |  |  |  |  |  |  |  |
| 17 |  |  |  |  |  |  |  |  |



Order quantities: $\mathrm{Q}=80$ units, $\mathrm{Q}=120$ units or $\mathrm{Q}=160$. Perform the following:
a. Data Table for 500 simulation runs: give the average of net profits, standard deviation, 95\% confidence interval.
b. Make a histogram for $G(Q, D)$ of the best $Q$ only

## Application \#2:

Patients arrive to a dental clinic according to a random process. The patients are served as first come first served bases. If the patient arrive and find the dentist busy he waits for his turn. Assume that the waiting room is infinite. Simulate this application under the following cases.

| G5 | $\cdots:$ | $\checkmark f_{x} \\|$ Patie | Wait?? |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4 | B | c | D | E | F | G | H | 1 | J |
| 1 | Dental clinic |  |  |  |  |  |  |  |  |
| 2 | Case 1 (a\&b) |  |  |  |  |  |  |  |  |
| 3 |  |  |  |  |  |  |  |  |  |
| 4 |  |  |  |  |  |  |  |  |  |
| 5 | Patient \# | Time Between Patients | Arrival Time | Service <br> Time | Service Start Time | Patient <br> Wait?? | Waiting <br> Time | Dep Time | Clinic Idle Time |
| 6 | 1 | 11.399 | 11.399 | 12 | 11.399 | 0 | 0 | 23.399 | 11.399 |
| 7 | 2 | 27.443 | 38.842 | 23 | 38.842 | 0 | 0.0000 | 61.842 | 15.443 |
| 8 | 3 | 19.728 | 58.570 | 11 | 61.842 | 1 | 3.2720 | 72.842 | 0.000 |
| 9 | 4 | 19.655 | 78.225 | 17 | 78.225 | 0 | 0.0000 | 95.225 | 5.383 |
| 10 | 5 | 13.537 | 91.762 | 13 | 95.225 | 1 | 3.4629 | 108.225 | 0.000 |
| 11 | 6 | 14.002 | 105.765 | 18 | 108.225 | 1 | 2.4605 | 126.225 | 0.000 |
| 12 | 7 | 13.708 | 119.473 | 14 | 126.225 | 1 | 6.7520 | 140.225 | 0.000 |
| 13 | 8 | 13.828 | 133.301 | 10 | 140.225 | 1 | 6.9238 | 150.225 | 0.000 |
| 14 | 9 | 15.175 | 148.476 | 38 | 150.225 | 1 | 1.7488 | 188.225 | 0.000 |
| 15 | 10 | 23.838 | 172.314 | 15 | 188.225 | 1 | 15.9108 | 203.225 | 0.000 |
| 16 | 11 | 13.569 | 185.884 | 18 | 203.225 | 1 | 17.3415 | 221.225 | 0.000 |
| 17 | 12 | 23.839 | 209.723 | 9 | 221.225 | 1 | 11.5024 | 230.225 | 0.000 |
| 18 | 13 | 14.768 | 224.491 | 9 | 230.225 | 1 | 5.7341 | 239.225 | 0.000 |
| 19 | 14 | 22.426 | 246.917 | 10 | 246.917 | 0 | 0.0000 | 256.917 | 7.692 |
| 20 | 15 | 11.109 | 258.026 | 32 | 258.026 | 0 | 0.0000 | 290.026 | 1.109 |
| 21 | 16 | 15.122 | 273.148 | 14 | 290.026 | 1 | 16.8785 | 304.026 | 0.000 |
| 22 | 17 | 27.222 | 300.370 | 15 | 304.026 | 1 | 3.6561 | 319.026 | 0.000 |
| 23 | 18 | 8.933 | 309.303 | 25 | 319.026 | 1 | 9.7235 | 344.026 | 0.000 |
| 24 | 19 | 17.862 | 327.165 | 8 | 344.026 | 1 | 16.8614 | 352.026 | 0.000 |
| 25 | 20 | 22.632 | 349.797 | 37 | 352.026 | 1 | 2.2296 | 389.026 | 0.000 |


|  | в | c | D | E | F | g | H |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Dental clinic |  |  |  |  |  |  |  |
|  |  | Case 1 (a\&b) |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
|  | Patient $\#$ | Time Between Patients | Arrival Time | Service Time | Service Start Time | Patient Wait?? | Waiting Time | Dep Time | Clinic Idle Time |
| 6 | 1 | $=-10^{*}$ LN(1-RAND())+RANDBETWEEN( 8,15 ) | =C6 | $=1 \mathrm{NT}\left(-15^{*}\right.$ L $\left.\operatorname{(1-RAND}()\right)+5$ | =D6 | 0 | 0 | =D6+E6+H6 | =D6 |
| 7 | 2 | $=-10 *$ LN(1-RAND() $)$ +RANDBETWEEN( 8,15 ) | =C7+D6 | $=1$ TT(-15*L $(1-\operatorname{RAND}())+5$ | $=1 F(16<=D 7, D 7,16)$ | $=1 F(D 7>16,0,1)$ | $=1 / F(G 7,16-\mathrm{D}, 0)$ | = D7+E7+H7 | $=1 F(D 7>16,07-16,0)$ |
| 8 | 3 | $=-10 *$ LN(1-RAND() $)$ +RANDBETWEEN( 8,15 ) | $=C 8+D 7$ | $=1$ NT(-15*L $(1-\operatorname{RAND}())+5$ | $=1 F(17<=D 8,08,77)$ | $=1 F(D 8 \gg 17,0,1)$ | $=1 F(G 8,17-\mathrm{D}, 00$ | =D8+E8+H8 | $=1 F(08>17,08-17,0)$ |
| 9 | 4 | $=-10 *$ LN(1-RAND() $)+$ RANDBETWEEN( 8,15 ) | =C9+D8 | $=1 \mathrm{NT}\left(-15^{*}\right.$ L $(1$ (1-RAND ()) ) +5 | $=1 F(18<=D 9,09,18)$ | $=1 F(D 9>18,0,1)$ | $=1 F(G 9,18-\mathrm{Dq}, 0)$ | = D9+E9+H9 | $=1 \mathrm{~F}(\mathrm{D9} 78, \mathrm{D} 9-18,0)$ |
| 0 | 5 | $=-10^{*}$ LN(1-RAND() $)+$ RANDBETWEEN( 8,15 ) | $=C 10+D 9$ | $=1 \mathrm{NT}\left(-15^{*}\right.$ L $(1$ (1-RAND () ) $)+5$ | $=I F(19<=D 10, D 10,19)$ | $=1 F(\operatorname{D10}>19,0,1)$ | =IF(G10,19-D10,0) | =D10+E10+H10 | $=1 F($ D10 19, D10-19,0) |
| 1 | 6 | $=-10^{*}$ LN(1-RAND() $)$ +RANDBETWEEN(8,15) | = C11+D10 | $=1 N T\left(-15^{*}\right.$ L $(1-$ RAND () ) $)+5$ | $=I F(110<=D 11, D 11,110)$ | $=1 F(\mathrm{D} 11>10,0,1)$ | $=1 F(611,110-\mathrm{D} 11,0)$ | = D11+E11+H11 | $=1 F(\mathrm{D} 11>110, \mathrm{D} 11-110,0)$ |
| 2 | 7 | $=-10^{*}$ LN(1-RAND() $)$ +RANDBETWEEN( 8,15 ) | $=C 12+$ D11 | $=1$ NT $\left(-15^{*}\right.$ L $(1-\operatorname{RAND}())+5$ | $=\mid F(111<=D 12, D 12,111)$ | $=1 F(\mathrm{D} 12>111,0,1)$ | $=\mid F(G 12,111-\mathrm{D} 12,0)$ | $=\mathrm{D} 12+$ E12+H12 | $=1 \mathrm{~F}(\mathrm{D} 12>111, \mathrm{D} 12-111,0)$ |
| 3 | 8 | $=-10^{*}$ LN(1-RAND() $)+$ RANDBETWEEN( 8,15 ) | $=C 13+D 12$ | $=1 \mathrm{NT}\left(-15^{*}\right.$ L $(1$ (1-RAND () ) $)+5$ | $=I F(12<=D 13, D 13,112)$ | $=\mathrm{IF}(\mathrm{D} 13>122,0,1)$ | $=1 F(G 13,112-\mathrm{D} 13,0)$ | $=\mathrm{D} 13+$ E13+H13 | $=I F(\mathrm{D} 13>112, \mathrm{D} 13-112,0)$ |
| 4 | 9 | $=-10 *$ LN(1-RAND() $)+$ RANDBETWEEN( 8,15 ) | = C14+D13 | $=1 \mathrm{NT}\left(-15^{*}\right.$ L $(1-$ RAND ()$)+5$ | $=1 F(133<=D 14, D 14,113)$ | $=1 F(\mathrm{D} 14>13,0,1)$ | $=1 F(G 14,113-\mathrm{D} 14,0)$ | = D14+E14+H14 | $=I F(D 14>113, D 14-113,0)$ |
| 5 | 10 | $=-10 *$ LN(1-RAND() $)$ +RANDBETWEEN( 8,15 ) | $=C 15+D 14$ | $=1 \mathrm{NT}\left(-15^{*} \operatorname{LN}(1-\mathrm{RAND}())+5\right.$ | $=1 F(14<=D 15, D 15,114)$ | $=1 F(\mathrm{D} 15>114,0,1)$ | $=1 F(G 15,114-D 15,0)$ | $=$ D15+E15+H15 | $=1 F(\mathrm{D} 15>114, \mathrm{D} 15-114,0)$ |

## Case-I

- Service time: time (in minutes) that follows integer exponential with mean $=15$ minutes and shift parameter $\delta=5$ minutes.( use integer function int(...))
- Arrival Process: The time between arrivals is exponential with mean $=10$ and shift parameter $\delta$ where $\delta \sim \operatorname{DU}[8,15]$ minutes
a. Data Table for 100 simulation runs, each run has 100 arrivals: Give the Average of (i), (ii) and(iii), standard deviation and 95\% confidence interval.
i. The average waiting time for a patient if he wait.
ii. The percentage that there is no patients in the clinic.
iii. The average number of patients served per hour.

Avg WT

| Average | 55.737 | 0.1276 | 2.7246 |
| :---: | :---: | :---: | :---: |
| STDV | 33.214 | 0.0640 | 0.1454 |
| LB-95\% | 49.147 | 0.1149 | 2.6958 |
| UB-95\% | 62.327 | 0.1403 | 2.7535 |


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| :---: | :---: | :---: | :---: |
|  | Avg WT | prob. no patient | avg \# patients served/h |
| Average | 55.259 | 0.1273 | 2.7295 |
| STDV | 33.579 | 0.0618 | 0.1178 |
| LB-95\% | 48.596 | 0.1151 | 2.7062 |
| UB-95\% | 61.922 | 0.1396 | 2.7529 |

## Avg WT prob. no patient avg \# patients served/h

| Average | 58.009 | 0.1222 | 2.7124 |
| :---: | :---: | :---: | :---: |
| STDV | 32.981 | 0.0611 | 0.1192 |
| LB-95\% | 51.465 | 0.1101 | 2.6887 |
| UB-95\% | 64.553 | 0.1343 | 2.7361 |

b. The distribution of number of patients in the system $N(t)$ for $N=0,1,2,3,4,5,6,7,8,9,10$ only.

| $\mathbf{N}(\mathbf{t})$ | $\mathbf{P}(\mathbf{N}(\mathrm{t}) \boldsymbol{)}$ |
| :---: | :---: |
| $\mathbf{0}$ | 0.1821 |
| $\mathbf{1}$ | 0.2820 |
| $\mathbf{2}$ | 0.1822 |
| $\mathbf{3}$ | 0.1255 |
| $\mathbf{4}$ | 0.1063 |
| $\mathbf{5}$ | 0.0639 |
| $\mathbf{6}$ | 0.0448 |
| $\mathbf{7}$ | 0.0128 |
| $\mathbf{8}$ | 0 |
| $\mathbf{9}$ | 0 |
| $\mathbf{1 0}$ | 0 |


| $\mathrm{N}(\mathrm{t})$ | $\mathrm{P}(\mathrm{N}(\mathrm{t}) \mathrm{I}$ |
| :---: | :---: |
| 0 | 0.06 |
| 1 | 0.14 |
| 2 | 0.09 |
| 3 | 0.05 |
| 4 | 0.12 |
| 5 | 0.27 |
| 6 | 0.13 |
| 7 | 0.09 |
| 8 | 0.04 |
| 9 | 0.00 |
| 10 | 0.00 |
| sum | $\mathbf{1 . 0 0}$ |

## Case-II

- Service Time:

| Service Type | Percentage Patients | Service time |
| :--- | :--- | :--- |
| Service 1 | $45 \%$ of the patients | Discrete uniform [10, 20] |
| Service 2 | $35 \%$ of the patients | integer exponential with mean $=15$ minutes <br> and shift parameter $\delta=5$ (use int(..) ) |
| Service 3 | $20 \%$ 0f the patients | Integer Gamma dist. With $\alpha=5$ and $\beta=4$ |

- Arrival Process: The time between arrivals is exponential with mean $=10$ and shift parameter $\delta$ where $\delta \sim \operatorname{DU}[8,15]$ minutes



Data Table for 100 simulation runs, each run has 100 arrivals: Give the Average of (i), (ii) and(iii), standard deviation and 95\% confidence interval.
i. The average waiting time for a patient if he wait.
ii. The percentage that there is no patients in the clinic.
iii. The average number of patients served per hour.

Avg WT prob. no patient avg \# patients served/h

| Average | 24.774 | 0.197 | 2.776 |
| :---: | :---: | :---: | :--- |
| STDV | 14.810 | 0.056 | 0.125 |
| LB-95\% | 21.835 | 0.186 | 2.751 |
| UB-95\% | 27.713 | 0.208 | 2.801 |

Avg WT prob. no patient avg \# patients served/h

| Average | 24.683 | 0.197 | 2.758 |
| :---: | :---: | :---: | :---: |
| STDV | 13.250 | 0.047 | 0.127 |
| LB-95\% | 22.054 | 0.188 | 2.733 |
| UB-95\% | 27.312 | 0.207 | 2.783 |

## Avg WT prob. no patient avg \# patients served/h

| Average | 24.958 | 0.206 | 2.754 |
| :---: | :---: | :---: | :--- |
| STDV | 14.846 | 0.060 | 0.139 |
| LB-95\% | 22.012 | 0.194 | 2.726 |
| UB-95\% | 27.903 | 0.218 | 2.782 |

