

College of Science.
Department of Statistics & Operations
Research

معيد الإحصاء وبحوث العمليات

First Midterm Exam Academic Year 1442-1443 Hijri-First Semester

	ئان Exam Information	معلومات الامة	
Course name	Modeling and Simulation	التمنجة والمحلكاذ	اسم المقرر
Course Code	OPER 441	441	
Exam Date	20-10-2021	14-3-1443	رمز المقرر تاريخ الامتحان
Exam Time	12: 00 P		وقت الامتحان
Exam Duration	2.5 hours	ساعتان ونصف	مدة الامتحان
Classroom No.			رقم قاعة الافتيار
Instructor Name			اسم استاذ المقرر

Student Informa	معلومات الطالب ition		
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ID number	4 38200235	الرقم الجامعي	
Section No.		رقم أنشعبة	
Serial Number		الوقع التسلسلي	
General Instructions:		تعليمات عامة:	
 Your Exam consists of PAGES (except this paper) Keep your mobile and smart watch out of the classroom. 	الامتحال معقدة (الإستنداء هذه النف والساعات الذكرة خارج فاعة الامتحال	 عند منفحات آ الورقة إ پچك إنقاء الهو 	

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#	Course Learning Outcomes (CLOs)	Related Question (s)	Points	Final Score
1	Understanding the processes and steps for building a simulation model			<u></u>
2	Implement an inverse cumulative distribution function based random variate generation algorithm			
3	Explain and implement the convolution algorithm for random variate generation			
4	Explain and implement the acceptance rejection algorithm for random variate generation			
5	Compute statistical quantities from simulation output			
6				
ř	Building simulation models from basic applications		†	
8		·		

EXAM COVER PAGE



Question #1: Answer the following with True or False:

<u> </u>	uesti	on #1: Answer the following with True or False:
1 1 2	-alse	 Simulation model can be used to evaluate different alternatives and give an optimal solution.
P	alse	The sample space in a random experiment is always determined and unique to everyone.
1	rue	3. Simulation modeling is not good if there is less data or no estimates available.
1	alse	4. Validation step is to make sure that the simulation program is running correctly.
i Fo	2/56	5. In call center model with two lines it is impossible to lose any incoming call.
TV	full	6. Triangular distribution is used when there is lack of data
F	else	7. Simulating flight distance for an airplane is a discrete system simulation.
	rue	8. In Bank simulation, the variable (X = number of customers in waiting) is a state variable for the system.
4	else	In Bank simulation, the variable (X = number of kids with a customer) is a state variable for the system.
Tr	rue	10. The measures of simulation changes every time a new run of simulation is performed
1-00	1se	11. Every simulation run for the same model give the same results.
1	rue	12. The Geometric distribution has memory less property
Fa	dse	13. If a used computer didn't fail for the past 6 months then the probability that it will not fail the next month is always the same as buying a new computer now.
T	ne	14. The normal distribution with parameters μ and σ^2 always cover more than 80% of the distribution within $\pm 2\sigma$
<u> </u>	a se	15. The Erlang distribution is a special case from exponential distribution.
<u> </u>	ue	16. We can always get any Erlang distribution with any parameters using Gamma <u>Distribution</u>
Fal	1 se	17. The beta distribution between (0,1) can be rescaled for any real values
Tn		18. The Erlang distribution always has all parameters positive integer values.
Tr		 The random variable with Exponential distribution is always has mean value equals t the standard deviation.
Tro	12	20. If the random variable has mean value equals to the variance then it must have a Poisson distribution.
I-als	se	21. The number of trials until 1st 2 success is a binomial distribution.

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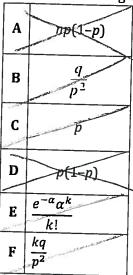
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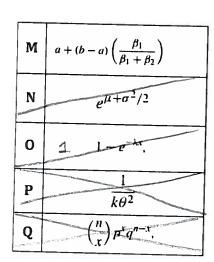
False	22. The Uniform distribution has a single mode value.
Frue	23. The normal distribution always has the mean equals to the median
	The state of the s

Question #2:

Given the following functions:



Ction.	
G	$\Gamma(\beta) = \int_0^\infty x^{\beta - 1} e^{-x} dx$
Н	$rac{\lambda^k x^{k-1} e^{-\lambda x}}{(k-1)!} ext{for } x, \lambda \geq 0,$
I	$\frac{1}{\sigma\sqrt{2\pi}}\exp\left[-\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2\right]$
J	$\frac{\beta}{\alpha} \left(\frac{x - \nu}{\alpha} \right)^{\beta - 1} \exp \left[-\left(\frac{x - \nu}{\alpha} \right)^{\beta} \right], x \ge \nu$
К	$\frac{\beta\theta}{\Gamma(\beta)}(\beta\theta x)^{\beta-1}e^{-\beta\theta x}, x>0$
L	$\frac{1}{\sqrt{2\pi}\sigma x}\exp\left[-\frac{(\ln x - \mu)^2}{2\sigma^2}\right].$



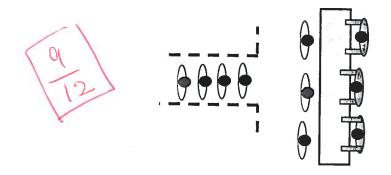
Complete the following by choosing the correct function from above

- 1	1	The random wasishing to	
A		The random variable X has Exponential distribution if if X has the CDF	1.0
1	2	The random variable X is has <i>Erlang</i> distribution if X has the pdf	10
	3	The random variable X has Beta distribution if X has the pdf	
	4	The random variable X has Geometric distribution (p) then X has the a variance	B
	5	The random variable X has <i>Lognormal</i> distribution if X has the <u>pdf</u>	المالية
	6	A random variable X has Negative binomial distribution(p) then X has the a variance	i de
	7	The random variable X has Beta distribution if X has the pdf	82
L	8	The random variable X has <i>Lognormal</i> distribution, Then X has expected value	W
	9	The random variable X has Beta distribution, then X has the expected value	4
	10	The random variable X has <i>Poisson</i> distribution if X has the pdf	
		The random variable X has Bernoulli distribution (p), then X has the expected value	LE .
1	12	The random variable X is has Erlang distribution (k) , then it has variance	ie i
	- 1	Alexandria management and	

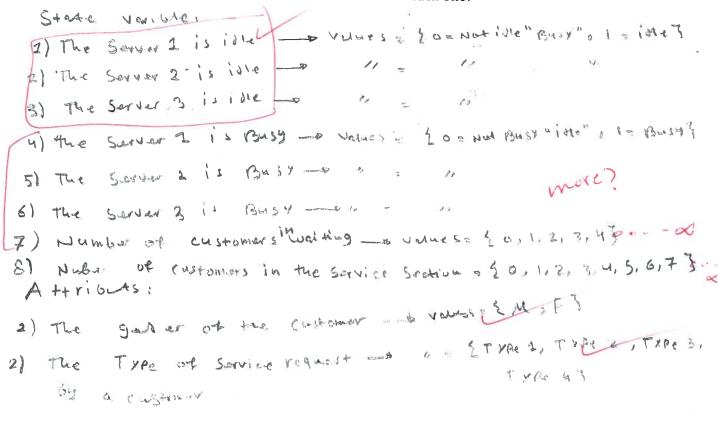


Question #3:

A service station has three servers and a single waiting line. The servers serve customers in the order in which they arrive. Customers may leave the system without service due to long waiting time. The service time of the customers changes according to their gender and the type of service they request. The service facility provide four types of services.



List al state variables and attributes and define the values of each one?





Question #4:

High temperature (°F) in a city on July 21, denoted by the random variable X, has the following probability density function, where X is in degrees F.



$$f(x) = \begin{cases} \frac{2(x-85)}{119}, & 85 \le x \le 92\\ \frac{2(102-x)}{170}, & 92 < x \le 102\\ 0, & \text{otherwise} \end{cases}$$

- (a) What is the mean of the temperature E(X)?
- (b) What is the variance of the temperature V(X)?
- (c) What is the median temperature?

(b) what is the inequal temperature?

(c) what is the inequal temperature?

(d)
$$E(x) = \int_{35}^{92} x \cdot \frac{2(x-85)}{119} dx + \int_{92}^{102} x \cdot \frac{170}{170} dx$$

$$= \frac{2}{119} \int_{85}^{102} x \cdot \frac{2(x-85)}{2} dx + \int_{130}^{102} x \cdot \frac{170}{2} dx$$

$$= \frac{2}{119} \left[-100157.3335 - (-102354.1667) \right] + \frac{2}{170} \left[1+6368 - 172101. \right]$$

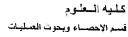
$$= \frac{2}{119} \left[-100157.3335 - (-102354.1667) \right] + \frac{2}{170} \left[1+6368 - 172101. \right]$$

$$= \frac{2}{119} \left[-100157.3335 - (-102354.1667) \right] + \frac{2}{170} \left[-102354.167 \right]$$

$$= \frac{2}{119} \left[-100157.3335 - (-102354.1667) \right] + \frac{2}{170} \left[-102354.167 \right] +$$

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Question #5:

Busses arrive to a station at random. It is estimated that the time between busses is an exponential distribution with mean 15 minutes. The number of passengers on the bus is also random follows a binomial distribution with parameter 10 and probability 0.75.

- (1) If you arrive at 10:00 am, What is the probability you will wait more than 30 min for your bus?
- (2) What is the expected number of busses that will arrive to the station between 10:00 to 11:00 am?
- (3) What is the expected number of passengers that will drop off to the station between 10:00 to 11:00 am?
- (4) Given that 15 passengers arrived between 10:00 to 11:00 am what is the probability that the next bus will have 3 passengers on board?
- (5) Draw the flowchart that will simulate the bus arrival and passenger's drop-off to this station? (Use the command Generate RV from Dist.-- to complete your flowchart)

(2) El number of Basser will environ between 10 am to 11 am)

@ E (number of Mes. that will drop of to the shapin)
= (10) (0:25) = 2.5 + 3 costomerx

(P (Next but will have 3 P. 1 15 Passi Willed 10mil)



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Question #6:

A supermarket sells fresh milk daily. Customers arrive to supermarket buy milk. Customers may buy 1 bottle, 2 bottle or 3 bottles at random (let B(j): number of bottles bought by customer j). The number of customers demanding the milk varies between 5 to 15 customers daily (let N(k): number customers arrived in day k asking for milk). The supermarket stores the milk in a refrigerator that can hold up to 20 bottles of milk. By the end of each day, the owner will decide wither to order more milk for next day or not. If he finds 10 or less in that the refrigerator then he will refill the refrigerator for next day.

Day	Cust-	Cust-	Cust-	Cust-	Cust- 5	Cust-	Cust-	Cust-	Cust-	Cust-	Cust-	Cust-	Cust-	Cust-	Cust-
	1	1	_ 2	1	3	_ 1	1	3	3	1	2	12	13	14	15
_2	1	3	1	_ 3	3	1	3	2	1	3	1	2	1		
3	_3_	1	3	2	1	2	1	1	1		1		1	3	3
4	2	3	1	2	3	3									
5	1	2	3	1	3	1	2	3					E 101		

(1) Draw the flowchart that will simulate number of sold bottles.

(2) Do the manual simulation to determine the status of customer (accepted, rejected) and

(3) From the manual simulation, estimate the number of sold units and the number of lost customers per day.

B(j): number of Bottles Bonger by Customer i jol, 1,8

N(H): " Customors domarding the modile i M=5,6,...,

deally between 5 to 15.

To or 1055 a refill

more than 10 - b Dow't retill

Dem 1

& Cust	A Bothles	Status	Amount of maint
1	1	accepted	TO CONTRACT OF THE PARTY OF THE
2	1	accepted	1.3
3	2	accepta	16
4	1	accepted	15
5	3	accumin	1.2
6	1	accepted	11
7	1	a (1000)	10
& Page 7 of 7	3	ac war w	lad.
9	Mark.	م دد دها	Ч
()	1	accupted !	3
11	2	accepted	1
POST (III) 1000PCTED DISHBOYSING SINCE	2 19		प्राचार र राज्य के हिन्दा संस्थापन के स्थापन के स्थापन के सम्बद्ध कर तह का उस की है। को किस्सा

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