

Third Semester  
(without calculators)  
Tuesday 12-10-1444

First Quiz  
Time: 30 mins.  
240 Math

King Saud University  
College of Science  
Math. Department

Name:

Univ. ID No.:

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Q1: If  $A = \begin{bmatrix} 1 & 3 \\ -1 & -1 \end{bmatrix}$ ,  $B = [1 \ 1 \ 1]$ , then find the following:

(a)  $A^{-1}$  (2 marks). (b)  $\text{tr}(A)$  (1 mark). (c)  $A^2$  (2 marks). (d)  $B^T B$  (2 marks).

Q2: Let A be the augmented matrix of a linear system. Find the solution of this system. (3 marks)

$$A = \begin{bmatrix} 1 & 2 & 3 & 5 \\ 1 & 3 & 3 & 5 \\ 1 & 2 & 4 & 5 \\ 2 & 4 & 6 & 10 \end{bmatrix}$$

## Solution

Q1:

$$(a) A^{-1} = \frac{1}{-1+3} \begin{bmatrix} -1 & -3 \\ 1 & 1 \end{bmatrix} = \frac{1}{2} \begin{bmatrix} -1 & -3 \\ 1 & 1 \end{bmatrix}$$

$$(b) \operatorname{tr}(A) = 1 - 1 = 0$$

$$(c) A^2 = AA = \begin{bmatrix} 1 & 3 \\ -1 & -1 \end{bmatrix} \begin{bmatrix} 1 & 3 \\ -1 & -1 \end{bmatrix} = \begin{bmatrix} -2 & 0 \\ 0 & -2 \end{bmatrix}$$

$$(d) B^T B = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} \begin{bmatrix} 1 & 1 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$

Q2:

$$\begin{aligned} A &= \begin{bmatrix} 1 & 2 & 3 & 5 \\ 1 & 3 & 3 & 5 \\ 1 & 2 & 4 & 5 \\ 2 & 4 & 6 & 10 \end{bmatrix} \xrightarrow{\substack{(-1)R_{12} \\ (-1)R_{13} \\ (-2)R_{14}}} \begin{bmatrix} 1 & 2 & 3 & 5 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} \\ &\xrightarrow{(-2)R_{21}} \begin{bmatrix} 1 & 0 & 3 & 5 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} \xrightarrow{(-3)R_{31}} \begin{bmatrix} 1 & 0 & 0 & 5 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} \\ &\Rightarrow (x_1, x_2, x_3) = (5, 0, 0) \end{aligned}$$