

**Pooled-Variance  $t$  Test for the Difference Between Two Means**

$$t_{STAT} = \frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\sqrt{S_p^2 \left( \frac{1}{n_1} + \frac{1}{n_2} \right)}} \quad (10.1)$$

**Confidence Interval Estimate for the Difference Between the Means of Two Independent Populations**

$$(\bar{X}_1 - \bar{X}_2) \pm t_{\alpha/2} \sqrt{S_p^2 \left( \frac{1}{n_1} + \frac{1}{n_2} \right)} \quad (10.2)$$

or

$$\begin{aligned} (\bar{X}_1 - \bar{X}_2) - t_{\alpha/2} \sqrt{S_p^2 \left( \frac{1}{n_1} + \frac{1}{n_2} \right)} &\leq \mu_1 - \mu_2 \\ &\leq (\bar{X}_1 - \bar{X}_2) + t_{\alpha/2} \sqrt{S_p^2 \left( \frac{1}{n_1} + \frac{1}{n_2} \right)} \end{aligned}$$

**Paired  $t$  Test for the Mean Difference**

$$t_{STAT} = \frac{\bar{D} - \mu_D}{\frac{S_D}{\sqrt{n}}} \quad (10.3)$$

**Confidence Interval Estimate for the Mean Difference**

$$\bar{D} \pm t_{\alpha/2} \frac{S_D}{\sqrt{n}} \quad (10.4)$$

or

$$\bar{D} - t_{\alpha/2} \frac{S_D}{\sqrt{n}} \leq \mu_D \leq \bar{D} + t_{\alpha/2} \frac{S_D}{\sqrt{n}}$$

### Z Test for the Difference Between Two Proportions

$$Z_{STAT} = \frac{(p_1 - p_2) - (\pi_1 - \pi_2)}{\sqrt{\bar{p}(1 - \bar{p})\left(\frac{1}{n_1} + \frac{1}{n_2}\right)}} \quad (10.5)$$

### F Test Statistic for Testing the Ratio of Two Variances

$$F_{STAT} = \frac{S_1^2}{S_2^2} \quad (10.7)$$

### $\chi^2$ Test for the Difference Between Two Proportions

$$\chi_{STAT}^2 = \sum_{\text{all cells}} \frac{(f_o - f_e)^2}{f_e} \quad (11.1)$$

#### Computing the Estimated Overall Proportion for $c$ Groups

$$\bar{p} = \frac{X_1 + X_2 + \dots + X_c}{n_1 + n_2 + \dots + n_c} = \frac{X}{n} \quad (11.3)$$

### Confidence Interval Estimate for the Difference Between Two Proportions

$$(p_1 - p_2) \pm Z_{\alpha/2} \sqrt{\left(\frac{p_1(1 - p_1)}{n_1} + \frac{p_2(1 - p_2)}{n_2}\right)} \quad (10.6)$$

or

$$\begin{aligned} (p_1 - p_2) - Z_{\alpha/2} \sqrt{\frac{p_1(1 - p_1)}{n_1} + \frac{p_2(1 - p_2)}{n_2}} &\leq (\pi_1 - \pi_2) \\ &\leq (p_1 - p_2) + Z_{\alpha/2} \sqrt{\frac{p_1(1 - p_1)}{n_1} + \frac{p_2(1 - p_2)}{n_2}} \end{aligned}$$

#### Computing the Estimated Overall Proportion for Two Groups

$$\bar{p} = \frac{X_1 + X_2}{n_1 + n_2} = \frac{X}{n} \quad (11.2)$$

#### Computing the Expected Frequency

$$f_e = \frac{\text{Row total} \times \text{Column total}}{n} \quad (11.4)$$