

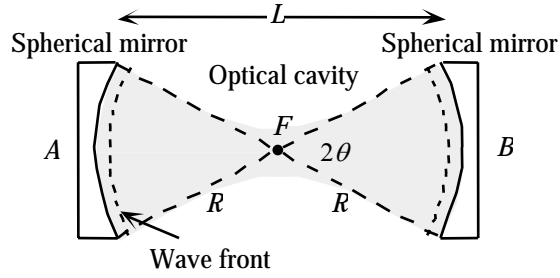


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**الاختبار النهائي لمقرر ٥٣١ فيز (الفصل الدراسي الثاني ١٤٢٧/١٤٢٨ هـ)**

Question one

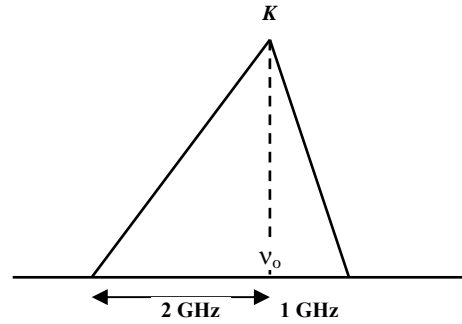
(a) In the confocal cavity shown, the light beam in the cavity is a Gaussian beam. If  $R = 25$  cm, and the mirrors are of diameter 2.5 cm, estimate the divergence of the beam and its spot size (minimum waist) for light of wavelength 500 nm.



(b) For inhomogeneous line shape function shown of the laser with;

$$\lambda = 8 \times 10^{-5} \text{ cm}, A_{21} = 2.5 \times 10^6 \text{ s}^{-1}, n = 2.75$$

Calculate the stimulated emission cross section.



Question Two

Consider a two-level system, non-degenerate, homogeneously broadened system of atoms with line-shape function  $g(\nu)$  and energy levels  $E_1$  and  $E_2$ . This system is pumped in a steady-state by monochromatic radiation with intensity  $I_\nu$  and frequency  $\nu = (E_2 - E_1)/h$ .

- (a) give stimulated transition rate  $W_{21}$  in terms of the pump intensity  $I_\nu$  and other atomic parameters.
- (b) Derive a steady-state expression for  $(N_1 - N_2)/(N_1 + N_2)$  of this system in terms of  $W_{12}$ ,  $W_{21}$  and  $A_{21}$ .  $N_1$  and  $N_2$  are the population density for the lower and upper state respectively;  $A_{21}$  is the spontaneous emission rate.

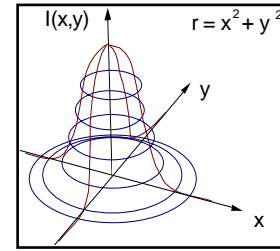
### Question Three

The electric field of a TEM<sub>00</sub> Gaussian beam may be expressed as follows;

$$E(x, y, z) = E_0 \times \frac{w_0}{w(z)} \exp\left[-\frac{r^2}{w^2(z)}\right] \times \exp\left\{-i\left[kz - \eta(z) + \frac{\pi r^2}{2R(z)}\right]\right\}$$

where  $w(z) = w_0 \sqrt{1 + \left(\frac{z}{z_0}\right)^2}$ ,  $k = \frac{2\pi m}{\lambda_0}$ ,  $R(z) = z\left[1 + \left(\frac{z_0}{z}\right)^2\right]$

$$z_0 = \frac{\pi w_0^2}{\lambda_0}, \quad \eta(z) = \tan^{-1}\left(\frac{z}{z_0}\right)$$

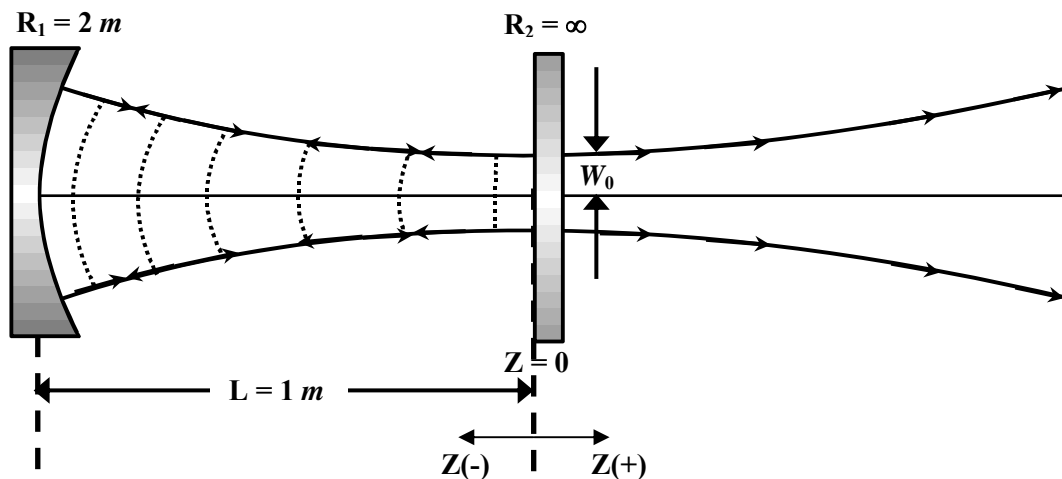


Describe briefly the physical consequences of the parameters,  $w_0$ ,  $z_0$ ,  $w(z)$ ,  $\eta(z)$  and  $R(z)$ , which make a Gaussian beam different from plane wave field  $E_0 \exp[i\omega t - ikz]$ .

### Question Four

Consider a 4 mW, TEM<sub>00</sub> He-Ne laser ( $\lambda = 632.8$  nm) with cavity dimensions given below. The left mirror ( $R_1 = 2$  m) is 100% reflecting. The right mirror ( $R_2 \rightarrow \infty$ ) is partially reflecting plain through which 4 mW output beam passes. The beam waist in the laser cavity ( $L = 1$  m) occurs at the plane mirror, where the reference plane  $z = 0$  was chosen.

- (a) Determine the spot size  $w_0$  at the beam waist.
- (b) Determine the laser beam spot size on the rear laser mirror.
- (c) Determine the complex radius of curvature  $\tilde{q}(z)$  at  $z = -1$  m and  $z = 0$ .
- (d) What is the half angle beam divergence  $\theta_{FF}$  for this laser in the far field?



### Question five

(a) Laser intensities are quoted in units of  $\text{W}/\text{cm}^2$ , and electric fields are quoted in units of  $\text{V}/\text{cm}$ .

(i) Give the numerical value of the electric field in a laser focus of  $100 \text{ W}/\text{cm}^2$  intensity (a relatively low power laser focused gently), in a focus of  $10^{19} \text{ W}/\text{cm}^2$  intensity (ultra high power laser focus).

(ii) For a 780 nm wavelength laser focused to  $10^{19} \text{ W}/\text{cm}^2$  intensity, what is the photon density (how many photons/s- $\text{cm}^2$  are passing through the focus)?



(b) The concept of oscillator strength  $f$  has been developed to provide a theoretical reference for the intensity of a spectroscopic transition. An absorption band in merocyanine dye has oscillator strength of 0.3 and an absorption maximum at 470 nm.

(I) Find the transition dipole moment.

(II) Find the Einstein B coefficient.

(III) Find the radiative lifetime.

مع تمنياتي لكم بالتوفيق والنجاح



#### PHYSICAL CONSTANTS

Rest mass of electron	$m$	$= 9.110 \times 10^{-31} \text{ kg}$
Charge of electron	$e$	$= 1.602 \times 10^{-19} \text{ C}$
Avogadro's constant	$N_A$	$= 6.022 \times 10^{23} \text{ mol}^{-1}$
Planck's constant	$h$	$= 6.626 \times 10^{-34} \text{ J s}$
Boltzmann's constant	$k$	$= 1.381 \times 10^{-23} \text{ J K}^{-1}$
Speed of light ( vacuum )	$c$	$= 2.998 \times 10^8 \text{ m s}^{-1}$
Stefan-Boltzmann constant	$\sigma_{\text{SB}}$	$= 5.670 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$