



جامعة الملك سعود
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قسم الفيزياء
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الرقم الجامعي

الاختبار النهائي لمقرر ٥٣١ فيز (الفصل الدراسي الأول ١٤٢٣/١٤٢٤ هـ)

1. (a) The quantum yield of $S_1 \rightarrow S_0$ transition for Rhodamine 6G is 0.87, and the corresponding lifetime is ≈ 5 ns. Calculate the radiative and nonradiative lifetimes (τ_{sp} and τ_{nr} , respectively) of the S_1 level (assume $\eta=1.36$ for ethanol).
(b) From a knowledge of the radiative life time τ_{sp} of Rhoamine 6G (from part a),
 - (i) Calculate the corresponding $|\mu|$, where $\lambda = 0.59 \mu\text{m}$ at the maximum of the emission curve.
 - (ii) Calculate the effective atomic dimension, a .
2. Consider a 488 nm Ar-ion gas laser. The tube length $L=1$ m, tube mirror reflectance are 99.9% and 95%. The linewidth $\Delta\nu=3$ GHz, the loss coefficient is $\alpha=0.1 \text{ m}^{-1}$, spontaneous decay time $\tau_{sp}=1/A_{21}=10$ ns and $\eta=1$.
 - (i) What is the threshold population inversion?
If the mirrors are concave and have radius of curvature equal to 1 m. calculate the beam diameter at;
 - (ii) The center of the laser.
 - (iii) At the mirrors.
 - (iv) At distance of 10 m from the laser.
 - (v) What is the divergence angle of the beam?
3. Consider a two-level system, non-degenerate, homogeneously broadened system of atoms with line-shape function $g(\nu)$ and energy levels E_1 and E_2 . This system is pumped in a steady-state by monochromatic radiation with intensity I_ν and frequency $\nu = (E_2-E_1)/h$.

- (a) give stimulated transition rate W_{21} in terms of the pump intensity I_ν and other atomic parameters.
- (b) Derive a steady-state expression for $(N_1-N_2)/(N_1+N_2)$ of this system in terms of W_{12} , W_{21} and A_{21} . N_1 and N_2 are the population density for the lower and upper state respectively; A_{21} is the spontaneous emission rate.
- (c) Can achieve population inversion for this system? If so, what is the necessary pump intensity I_ν ?
4. The R_1 laser transition of Ruby has a good approximation a Lorentzian shape of width (FWHM) 330 GHz at room temperature. The measured peak transition cross-section is $\sigma = 2.5 \times 10^{-20} \text{ cm}^2$. Calculate the radiative lifetime (the refractive index is $n=1.76$). Since the observed room temperature lifetime is 3 ms, what is the fluorescence quantum yield?
5. Derive the expression $A = \frac{16\pi^3 \nu_0^3 \eta |\mu|^2}{3h \epsilon_0 c^3}$ for the Einstein A coefficient, i.e. the rate of spontaneous emission.

PHYSICAL CONSTANTS

Rest mass of electron	m	$= 9.110 \times 10^{-31} \text{ kg}$
Charge of electron	e	$= 1.602 \times 10^{-19} \text{ C}$
Avogadro's constant	N_A	$= 6.022 \times 10^{23} \text{ mol}^{-1}$
Planck's constant	h	$= 6.626 \times 10^{-34} \text{ J s}$
Boltzmann's constant	k	$= 1.381 \times 10^{-23} \text{ J K}^{-1}$
Speed of light (vacuum)	c	$= 2.998 \times 10^8 \text{ m s}^{-1}$
Stefan-Boltzmann constant	σ_{SB}	$= 5.670 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$
Permittivity of a vacuum	ϵ_0	$= 8.854 \times 10^{-12} \text{ Fm}^{-1}$

مع تمنياتي لكم بالتوفيق والنجاح