

King Saud University  
Department of Mathematics  
M-203  
(Differential & Integral Calculus)  
First Mid-Term Examination  
Summer Term (1436)

Max. Marks: 25

Time: 90 minutes

Marks: Q.1[4]; Q.2[5]; Q.3[5]; Q.4[6]; Q.5[5]

Q.No: 1 Determine whether or not the sequence  $\left\{ \frac{n^2}{2n-1} - \frac{n^2}{2n+1} \right\}_{n=1}^{\infty}$  converges, and if it converges, find its limit.

Q. No: 2 Find the **sum** of the series  $\sum_{n=1}^{\infty} \left[ \frac{9}{(3n-1)(3n+2)} \right]$ .

Q. N0: 3 Determine whether the following series is **absolutely convergent, conditionally convergent** or **divergent**  $\sum_{n=1}^{\infty} \frac{(-1)^n}{\ln(n+1)}$ .

Q.No: 4 Find the interval of convergence and the radius of convergence of the power series:  $\sum_{n=0}^{\infty} (-3)^n \frac{x^n}{\sqrt{n+1}}$ .

Q. N0: 5 Find the first three non-zero terms of a Taylor series for  $f(x) = x^2 e^x$  at  $c = -1$ .