

Homework - IV

1. Show the **modulation property** of the Fourier transform.
2. Show that if a two dimensional sequence is **separable** then so is its Fourier transform, i.e., if $A(m, n) = A_1(m)A_2(n)$ then $F_A(w_1, w_2) = F_{A_1}(w_1)F_{A_2}(w_2)$ where $F_{A_1}(w_1), F_{A_2}(w_2)$ are *one* dimensional Fourier transforms such as $F_a(w) = \frac{1}{2\pi} \sum_{n=-\infty}^{+\infty} a(n)e^{-jwn}$.
3. Obtain the Fourier transform of the 2-D sequence $A(m, n)$ given by:

| | | | |
|---------|---------|----|----|
| | $n = 0$ | 1 | 2 |
| $m = 0$ | 1 | 2 | -1 |
| 1 | 2 | 4 | -2 |
| 2 | -1 | -2 | 1 |

Simplify your answer as much as possible.

4. Calculate the Fourier transform of the limited extent sequence $A(m, n) = 1, 0 \leq m < 8, 0 \leq n < 8$ and $A(m, n) = 0$ otherwise.
5. Calculate the Fourier transform of the limited extent sequence $A(m, n) = (-1)^{m+n}, 0 \leq m < 8, 0 \leq n < 8$ and $A(m, n) = 0$ otherwise.