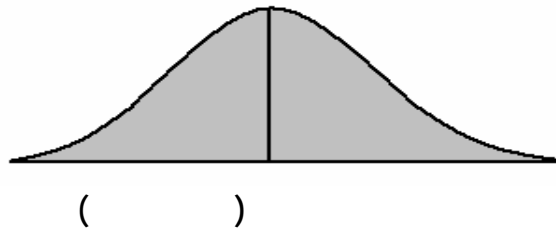


/



Skewness

/

:

"Person"

//

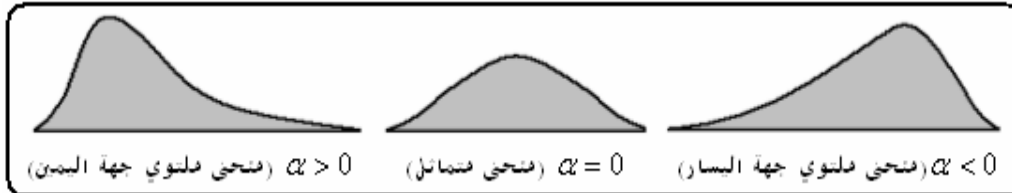
(-) :

المتوال = الوسط الحسابي - ٣(الوسط الحسابي - الوسيط)

(١-٥)

$$\alpha = \frac{3(\text{Mean} - \text{Median})}{\text{Standard Deviation}} = \frac{3(\bar{x} - \text{Med})}{S} \quad (٢-٥)$$

S	Med	\bar{x}	"	"	() α	
:						
		$(\alpha = 0)$	(=)	•
		$(\alpha > 0)$	(<)	•
		$(\alpha < 0)$	(>)	•
					(-)	



" " / /

100

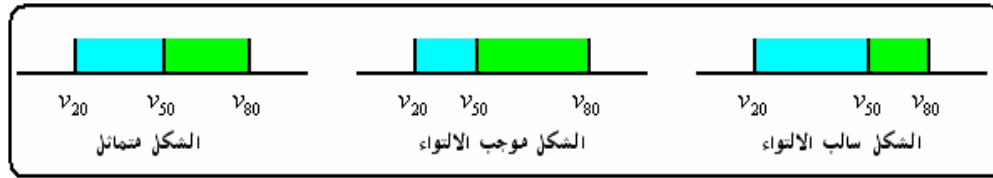
(v_{15})	15		
(v_p)	p	15%	
		:	
$x_{(1)} < x_{(2)} < \dots < x_{(n)}$:		•
	$R = (n+1) \left(\frac{p}{100} \right)$:	•
	$(v_{15} = x_{(R)})$	R	•
:	(v_p)	R	•

$$v_p = x_{(I)} + (R - i)(x_{(u)} - x_{(I)}) \quad (٣-٥)$$

$$\begin{matrix} v_{50} & & v_{100-p} & & v_p \\ & & & & 80 & & 20 \end{matrix}$$

:

(-)



:

$$\begin{matrix} (v_{50}) & & (v_{20}) & & (v_{50}) & & (v_{80}) & \bullet \\ (v_{50}) & & (v_{20}) & & (v_{50}) & & (v_{80}) & \bullet \\ (v_{50}) & & (v_{20}) & & (v_{50}) & & (v_{80}) & \bullet \end{matrix}$$

$$\alpha_{p,100-p} = \frac{(v_{100-p} - v_{50}) - (v_{50} - v_p)}{v_{100-p} - v_p} \quad (٤-٥)$$

$$v_p < v_{50} < v_{100-p} :$$

$$75 \quad (v_{25} = Q_1) \quad 25$$

:

$$(v_{75} = Q_3)$$

$$v_q = \frac{(Q_3 - Q_2) - (Q_2 - Q_1)}{(Q_3 - Q_1)} \quad (٥-٥)$$

(-)

8

66 85 52 78 80 91 74 58

• " " - :

• " " -
: (-)
:

x	x^2
66	4356
85	7225
52	2704
78	6084
80	6400
91	8281
74	5476
58	3364
584	43890

$\sum x = 584$, $\sum x^2 = 43890$

$\bar{x} = \frac{\sum x}{n} = \frac{584}{8} = 73$

$s = \sqrt{\frac{\sum x^2 - (\sum x)^2/n}{n-1}} = \sqrt{\frac{43890 - (584)^2/8}{8-1}}$
 $= \sqrt{\frac{1258}{7}} = \sqrt{179.71428} = 13.406$

: •

$(n+1)/2 = (8+1)/2 = 4.5$:

52 58 | 66 74 | 78 80 | 85 91
 1 2 | 3 4 | 5 6 | 7 8
 2.25 4.5 6.75

११

$$Med = 74 + 0.5(78 - 74) = 76$$

$$s.c = \frac{3(\bar{x} - Med)}{S} = \frac{3(73 - 76)}{13.406} = -0.67$$

(-)

$$(n+1)/4 = (8+1)(1/4) = 2.25 :$$

$$Q_1 = 58 + (2.25 - 2)(66 - 58) = 60$$

$$(n+1)/(3/4) = (8+1)(3/4) = 6.75 :$$

$$Q_3 = 80 + (6.75 - 6)(85 - 80) = 83.75$$

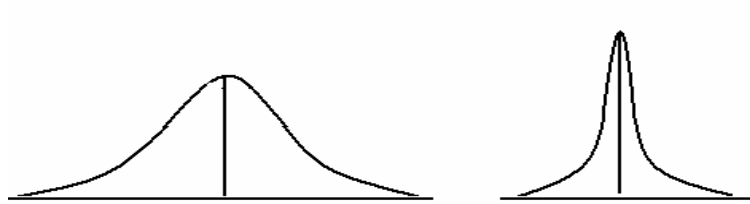
$$Med(Q_2) = 76$$

$$\begin{aligned} \alpha_q &= \frac{(Q_3 - Q_2) - (Q_2 - Q_1)}{(Q_3 - Q_1)} = \frac{(83.75 - 76) - (76 - 60)}{(83.75 - 60)} \\ &= \frac{-8.25}{23.75} = -0.35 \end{aligned}$$

...

Kurtosis

/



: (K)

$$k = \frac{\frac{1}{n} \sum (x - \bar{x})^4}{s^4}$$

(7-9)

s

$$\sum (x - \bar{x})^4 / n$$

3

:

k=3 •

k>3 •

k<3 •

$\bar{x} = 73$: (-)

x	66	85	52	78	80	91	74	58	584
$(x - \bar{x})$	-7	12	-21	5	7	18	1	-15	0
$(x - \bar{x})^2$	49	144	441	25	49	324	1	225	1258
$(x - \bar{x})^4$	2401	20736	194481	625	2401	104976	1	50625	376246

1.1

:

$$s = \sqrt{\frac{\Sigma(x - \bar{x})^2}{n-1}} = \sqrt{\frac{1258}{7}} = 13.406$$

$$\frac{1}{n} \Sigma (x - \bar{x})^2 = \frac{1}{8} (376246) = 47030.75$$

:

$$K = \frac{47030.75}{(13.406)^4} = \frac{47030.75}{32299.58} = 1.456$$

.

/

:

Variation Coefficient

//

:

$$v.c = \frac{s}{\bar{x}} \times 100$$

(V-9)

١٠٢

:

$$v.c_q = \frac{(Q_3 - Q_1) / 2}{Med} \times 100$$

(٨-٥)

(-)

$\bar{x} =$	173	198
$s =$	23	25

:

:

$$v.c_1 = \frac{s}{\bar{x}} \times 100 = \frac{23}{173} \times 100 = 13.3\%$$

:

$$v.c_2 = \frac{s}{\bar{x}} \times 100 = \frac{25}{195} \times 100 = 12.8\%$$

//

$$\frac{\text{المدى}}{4} > \text{الانحراف المعياري} > \frac{\text{المدى}}{6}$$
$$\frac{\text{Rang}}{6} < \hat{s} < \frac{\text{Rang}}{4}$$

(٩-٥)

۱.۳

Standardized degree

//

\bar{x} n x_1, x_2, \dots, x_n
 z x s
 :

$$z = \frac{x - \bar{x}}{s}$$

(۱-۰)

(-)
(-)

180

178

:

$\bar{x} =$	173	198
$s =$	23	25
.	178	180

.(-)

: (178 Kg.)

$$z = \frac{x - \bar{x}}{s} = \frac{178 - 173}{23} = 0.22$$

1.4

: (180 Kg.)

$$z = \frac{x - \bar{x}}{s} = \frac{180 - 198}{25} = -0.75$$

0.22

178

0.75

180

//

s

\bar{x}

x_1, x_2, \dots, x_n

:

$\bar{x} \pm s$

68%

$\bar{x} \pm 2s$

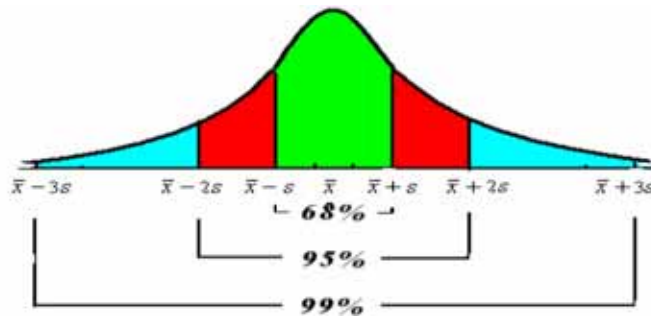
95%

$\bar{x} \pm 3s$

99%

:

(-)



" "

//

:

" "

$k > 1 \quad \bar{x} \pm ks$

$(1 - 1/k^2) \%$

$\bar{x} \pm 2s$

75%

$\bar{x} \pm 3s$

89%

Box Plot

" "

//

Q1

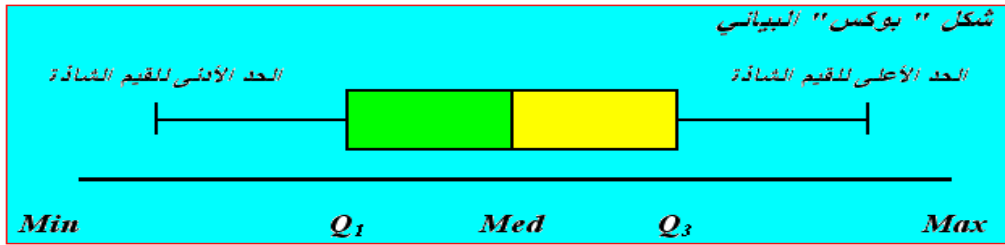
" "

١٠٥

Med () Q₃

: " "

(-)



: " "

Q₃ , Med :

Q₁ Med Q₁

Q₃ Med Q₃

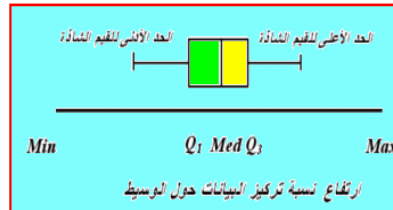
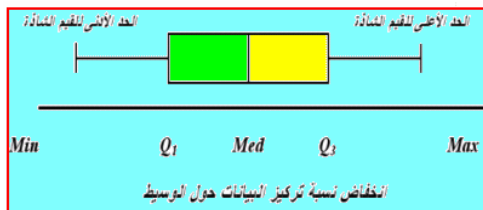
: Q₁

(-)



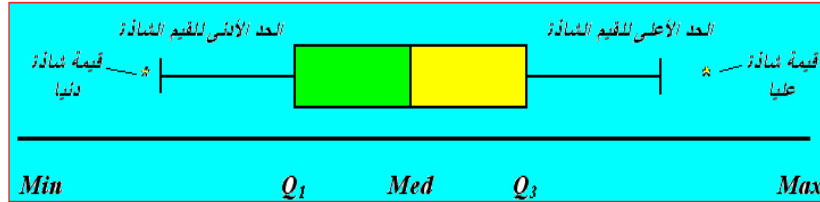
Box :

(-)



(*)

(-)



:

$$Q = (Q_3 - Q_1) / 2$$

$$Low = Q_1 - 3Q$$

$$UPP = Q_3 + 3Q$$

(-)

: 12

6 10 18 3 9 10 5 6 11 8 2 7

:

" "

" "

2 3 5 6 6 7 8 9 10 10 11 18

:

$$Min = 2$$

$$Max = 18$$

١٠٧

: Q₁

$$(n+1)(1/4)=(13/4)=3.25$$

$$Q_1 = 5 + 0.25(6 - 5) = 5.25 : Q_1$$

:Med

$$(n+1)(1/2)=(13/2)=6.5$$

$$Med = 7 + 0.5(8 - 7) = 7.5 : Med$$

:Q₃

$$(n+1)(3/4)=(13)(3/4)=9.75$$

$$Q_3 = 10 + 0.75(10 - 10) = 10 : Q_3$$

$$Q = (10 - 5.25) / 2 = 2.375 :$$

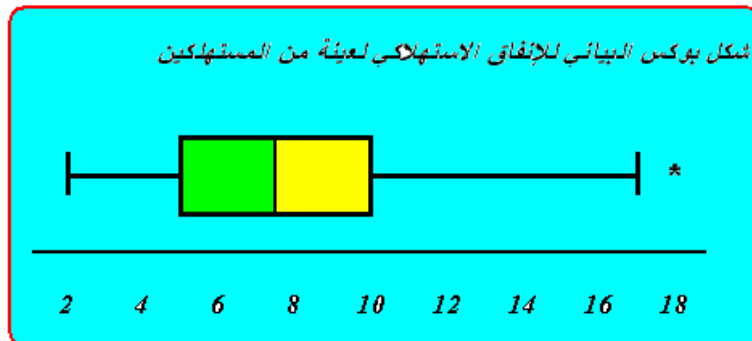
:

$$Low = Q_1 - 3Q = 5.25 - 3(2.375) = -1.875$$

:

$$Upp = Q_3 + 3Q = 10 + 3(2.375) = 17.125$$

" "



:

60%

.18

" "