

Brief solutions to selected problems from the textbook:  
 Note the correction to problem 7.3.1

6.4.1:  $n_1 = 5, \bar{x}_1 = 48, s_1 = 8.1; n_2 = 7, \bar{x}_2 = 56.7, s_2 = 8.1$

$$t_{10,0.95} = 1.8125, s_p^2 = \frac{4(8.1)^2 + 6(8.1)^2}{10} = 65.61, \sqrt{\frac{s_p^2}{5} + \frac{s_p^2}{7}} = 4.7429$$

$$\mu_1 - \mu_2 = (-8.7) \pm (8.5965) = (-17.2965, -0.1035)$$

6.4.2:  $n_1 = 8, \bar{x}_1 = 74, \sqrt{\frac{\sigma_1^2}{n_1}} = 6; n_2 = 12, \bar{x}_2 = 101, \sqrt{\frac{\sigma_2^2}{n_2}} = 5$

$$Z_{0.95} = 1.645, \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}} = \sqrt{36 + 25} = 7.8103$$

$$\mu_1 - \mu_2 = (-27) \pm (12.8479) = (-39.8479, -14.1521)$$

6.4.3:  $n_1 = 120, \bar{x}_1 = 21.4444, s_1 = 15.392; n_2 = 42, \bar{x}_2 = 3.3333, s_2 = 14.595$

$$Z_{0.95} = 1.645, \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}} = \sqrt{7.046} = 2.6544$$

$$\mu_1 - \mu_2 = (18.1111) \pm (4.3665) = (13.7446, 22.4776)$$

6.4.4:  $n_1 = 5, \bar{x}_1 = 6.02, s_1 = 1.217; n_2 = 5, \bar{x}_2 = 3.378, s_2 = 1.687$ ; equal vars.

$$t_{8,0.95} = 1.86, s_p^2 = \frac{4(1.217)^2 + 4(1.687)^2}{8} = 2.1635, \sqrt{\frac{s_p^2}{5} + \frac{s_p^2}{7}} = 0.9303$$

$$\mu_1 - \mu_2 = (2.642) \pm (1.7304) = (0.9116, 4.3724)$$

6.4.5:  $n_1 = 123, \bar{x}_1 = 0.83, \sqrt{\frac{\sigma_1^2}{n_1}} = 0.16; n_2 = 290, \bar{x}_2 = 1.39, \sqrt{\frac{\sigma_2^2}{n_2}} = 0.18$

$$Z_{0.95} = 1.645, \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}} = \sqrt{(0.16)^2 + (0.18)^2} = 0.2408$$

$$\mu_1 - \mu_2 = (-0.56) \pm (0.3961) = (-0.9561, -0.1639)$$

6.4.6:  $n_1 = 12, \bar{x}_1 = 13.21, s_1 = 1.05; n_2 = 9, \bar{x}_2 = 11, s_2 = 1.01$ ; equal vars.

$$t_{19,0.95} = 1.7291, s_p^2 = \frac{11(1.05)^2 + 8(1.01)^2}{19} = 1.0678, \sqrt{\frac{s_p^2}{12} + \frac{s_p^2}{9}} = 0.4557$$

$$\mu_1 - \mu_2 = (2.21) \pm (0.788) = (1.422, 2.998)$$

6.4.7:  $n_1 = 12, \bar{x}_1 = 11.1, s_1 = 1.5; n_2 = 12, \bar{x}_2 = 7.8, s_2 = 2$ ; equal vars.

$$t_{22,0.95} = 1.7171, s_p^2 = \frac{11(1.5)^2 + 11(2)^2}{22} = 3.125, \sqrt{\frac{s_p^2}{12} + \frac{s_p^2}{12}} = 0.7217$$

$$\mu_1 - \mu_2 = (3.3) \pm (1.2392) = (2.0608, 4.5392)$$

6.4.8:  $n_1 = 11, \bar{x}_1 = 26, s_1 = 5; n_2 = 14, \bar{x}_2 = 21, s_2 = 6$ ; equal vars.

$$t_{23,0.95} = 1.7139, s_p^2 = \frac{10(5)^2 + 13(6)^2}{23} = 31.2174, \sqrt{\frac{s_p^2}{11} + \frac{s_p^2}{14}} = 2.2512$$

$$\mu_1 - \mu_2 = (5) \pm (3.8583) = (1.1417, 8.8583)$$

6.4.9:  $n_1 = 20$ ,  $\bar{x}_1 = 7$ ,  $s_1 = 2$ ;  $n_2 = 24$ ,  $\bar{x}_2 = 36$ ,  $s_2 = 10$ ,  $w_1 = 0.2$ ,  $w_2 = 4.1667$

$$t_{19,0.95} = 1.7291, t_{23,0.95} = 1.7139, t' = 1.7146, \sqrt{w_1 + w_2} = 2.0897$$

$$\mu_1 - \mu_2 = (-29) \pm (3.583) = (-32.583, -25.417)$$

6.4.10:  $n_1 = 14$ ,  $\bar{x}_1 = 20.41$ ,  $s_1 = 6.81$ ;  $n_2 = 18$ ,  $\bar{x}_2 = 14.72$ ,  $s_2 = 6.2$ ; equal vars.

$$t_{30,0.95} = 1.6973, s_p^2 = \frac{13(6.81)^2 + 17(6.2)^2}{30} = 41.879, \text{s.e.} = \sqrt{\frac{s_p^2}{11} + \frac{s_p^2}{14}} = 2.3061$$

$\mu_1 - \mu_2 = (5.69) \pm (3.9141) = (1.7759, 9.6041)$ , yes, by between 1.8, and 9.6, because the interval does not include 0.

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6.5.1  $X = 166$ ,  $n = 947$ , p.e. =  $\hat{p} = 0.1753$ ,  $1 - \hat{p} = 0.8247$ , r.c. =  $Z_{0.95} = 1.645$ ,

$$\text{s.e.} = \sqrt{\frac{\hat{p}(1 - \hat{p})}{n}} = 0.01236; 90\% \text{ c.i.} = p = 0.1753 \pm 0.0203 = (0.155, 0.1956)$$

6.5.2  $n = 1229$ , p.e. =  $\hat{p} = 0.5$ ,  $1 - \hat{p} = 0.5$ , r.c. =  $Z_{0.975} = 1.96$ ,

$$\text{s.e.} = \sqrt{\frac{\hat{p}(1 - \hat{p})}{n}} = 0.01426; 95\% \text{ c.i.} = p = 0.5 \pm 0.02795 = (0.47205, 0.52795)$$

6.5.3  $n = 86$ , p.e. =  $\hat{p} = 0.128$ ,  $1 - \hat{p} = 0.872$ , r.c. =  $Z_{0.995} = 2.58$ ,

$$\text{s.e.} = \sqrt{\frac{\hat{p}(1 - \hat{p})}{n}} = 0.03603; 99\% \text{ c.i.} = p = 0.128 \pm 0.09296 = (0.03504, 0.22096)$$

6.5.4  $X = 88$ ,  $n = 125$ , p.e. =  $\hat{p} = 0.704$ ,  $1 - \hat{p} = 0.296$ , r.c. =  $Z_{0.975} = 1.96$ ,

$$\text{s.e.} = \sqrt{\frac{\hat{p}(1 - \hat{p})}{n}} = 0.04083; 95\% \text{ c.i.} = p = 0.704 \pm 0.08 = (0.624, 0.784)$$


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6.6.1  $X_1 = 145$ ,  $n_1 = 194$ ,  $\hat{p}_1 = 0.74742$ ,  $X_2 = 113$ ,  $n_2 = 189$ ,  $\hat{p}_2 = 0.59788$

$$\text{p.e.} = \hat{p}_1 - \hat{p}_2 = 0.14954, \text{r.c.} = Z_{0.975} = 1.96, \text{s.e.} = \sqrt{0.0022452} = 0.047384$$

$$p_1 - p_2 = 0.14954 \pm 0.092873 = (0.056667, 0.242413)$$

6.6.2  $n_1 = 404$ ,  $\hat{p}_1 = 0.592$ ,  $n_2 = 795$ ,  $\hat{p}_2 = 0.449$ , r.c. =  $Z_{0.995} = 2.58$ ,

$$\text{p.e.} = \hat{p}_1 - \hat{p}_2 = 0.143, \text{s.e.} = 0.030105$$

$$p_1 - p_2 = 0.14253 \pm 0.077671 = (0.064857, 0.2202)$$

6.6.3  $X_1 = 52$ ,  $n_1 = 67$ ,  $\hat{p}_1 = 0.77612$ ,  $X_2 = 89$ ,  $n_2 = 133$ ,  $\hat{p}_2 = 0.66917$

$$\text{p.e.} = \hat{p}_1 - \hat{p}_2 = 0.10695, \text{r.c.} = Z_{0.975} = 1.96, \text{s.e.} = \sqrt{0.0042578} = 0.0652515$$

$$p_1 - p_2 = 0.10695 \pm 0.12789 = (-0.02094, 0.23484)$$

6.6.4  $X_1 = 58$ ,  $n_1 = 215$ ,  $\hat{p}_1 = 0.269767$ ,  $X_2 = 217$ ,  $n_2 = 1140$ ,  $\hat{p}_2 = 0.190351$

$$\text{p.e.} = \hat{p}_1 - \hat{p}_2 = 0.079416, \text{r.c.} = Z_{0.95} = 1.645, \text{s.e.} = \sqrt{0.0010512} = 0.0324225$$

$$p_1 - p_2 = 0.079416 \pm 0.053335 = (0.02608, 0.132751)$$


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7.2.1  $n = 211$ ,  $\bar{x} = 59.1$ ,  $s = 25.6$ ;  $H_0 : \mu \geq 60$ ,  $H_1 : \mu < 60$ ;  $\alpha = 0.1$

$$z_0 = \frac{59.1 - 60}{\frac{25.6}{\sqrt{211}}} = -.51, z_{0.9} = 1.28, p = 0.305, \text{do not rej. } H_0, \text{no less than 60.}$$

7.2.2 n = 3918,  $\bar{x} = .9$ , s = .96;  $H_0 : \mu \geq 1$ ,  $H_1 : \mu < 1$ ;  $\alpha = 0.01$

$$z_0 = \frac{0.9 - 1}{\frac{0.96}{\sqrt{3918}}} = -.51, z_{0.99} = 2.33, p = 0.0, \text{ rej. } H_0, \text{ the mean is } < 1.$$

7.2.3 n = 8,  $\bar{x} = 25$ , s = 4;  $H_0 : \mu \leq 20$ ,  $H_1 : \mu > 20$ ;  $\alpha = 0.01$

$$t_0 = \frac{25 - 20}{\frac{4}{\sqrt{8}}} = 3.54, t_{7,0.99} = 3, p = 0.005, \text{ rej. } H_0, \text{ the mean is } > 20.$$

7.2.4 n = 25,  $\bar{x} = 4.8$ , s = 2;  $H_0 : \mu \leq 4$ ,  $H_1 : \mu > 4$ ;  $\alpha = 0.05$

$$t_0 = \frac{4.8 - 4}{\frac{2}{\sqrt{24}}} = 2, t_{24,0.95} = 1.71, p = 0.028, \text{ rej. } H_0, \text{ the mean is } > 4.$$

7.2.5 n = 49,  $\bar{x} = 21$ , s = 11;  $H_0 : \mu \geq 30$ ,  $H_1 : \mu < 30$ ;  $\alpha = 0.05$

$$z_0 = \frac{21 - 30}{\frac{11}{\sqrt{7}}} = -5.73, z_{0.95} = 1.645, p = 0.0, \text{ rej. } H_0, \text{ the mean is } < 30.$$

7.2.6 n = 9,  $\bar{x} = 6.5$ , s = 0.6;  $H_0 : \mu \leq 6$ ,  $H_1 : \mu > 6$ ;  $\alpha = 0.05$

$$t_0 = \frac{6.5 - 6}{\frac{0.6}{\sqrt{9}}} = 2.5, t_{8,0.95} = 1.86, p = 0.018, \text{ rej. } H_0, \text{ the mean is } > 6.$$

7.2.7 n = 25,  $\bar{x} = 77$ , s = 10;  $H_0 : \mu \geq 80$ ,  $H_1 : \mu < 80$ ;  $\alpha = 0.05$

$$t_0 = \frac{77 - 80}{\frac{10}{\sqrt{25}}} = -1.5, t_{24,0.95} = 1.71, p = 0.073, \text{ do not rej. } H_0, \text{ the mean is } < 80.$$


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7.3.1  $n_1 = 79$ ,  $\bar{x}_1 = 2.1$ ,  $s_1 = 1.1$ ;  $H_0 : \mu_1 \leq \mu_2, \mu_1 - \mu_2 \leq 0$ ;  $\alpha = 0.01$

$n_2 = 74$ ,  $\bar{x}_2 = 1.6$ ,  $s_2 = 1.2$ ;  $H_1 : \mu_1 > \mu_2, \mu_1 - \mu_2 > 0$

$$z_0 = \frac{2.1 - 1.6}{\sqrt{\frac{1.1^2}{79} + \frac{1.2^2}{74}}} = 2.68121, z_{0.99} = 2.33, p = 0.004, \text{ rej. } H_0, \mu_1 > \mu_2$$

7.3.2  $n_1 = 11$ ,  $\bar{x}_1 = 7116$ ,  $\sqrt{\frac{\sigma_1^2}{n_1}} = 173$ ;  $n_2 = 11$ ,  $\bar{x}_2 = 7058$ ,  $\sqrt{\frac{\sigma_2^2}{n_2}} = 205$ ;

$H_0 : \mu_1 \leq \mu_2, \mu_1 - \mu_2 \leq 0$ ;  $\alpha = 0.05$ ;  $H_1 : \mu_1 > \mu_2, \mu_1 - \mu_2 > 0$

$$z_0 = \frac{\bar{x}_1 - \bar{x}_2}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}} = \frac{58}{268.2424} = 0.2162, z_{0.95} = 1.645, p = 0.414, \text{ do not rej. } H_0,$$

7.3.3  $n_1 = 16$ ,  $\bar{x}_1 = 6218$ ,  $s_1 = 693$ ;  $H_0 : \mu_1 = \mu_2, \mu_1 - \mu_2 = 0$ ;  $\alpha = 0.05$

$n_2 = 16$ ,  $\bar{x}_2 = 8421$ ,  $s_2 = 1398$ ;  $H_1 : \mu_1 \neq \mu_2, \mu_1 - \mu_2 \neq 0$

$$t_0 = \frac{6218 - 8421}{\sqrt{\frac{693^2}{16} + \frac{1398^2}{16}}} = -5.65, \quad t' = t_{15,0.975} = 2.1315, \quad p = 0.0, \quad \text{rej. } H_0,$$

7.3.4  $n_1 = 16, \bar{x}_1 = 22.5, s_1 = 4.1; H_0 : \mu_1 \geq \mu_2, \mu_1 - \mu_2 \geq 0 ; \alpha = 0.05$   
 $n_2 = 21, \bar{x}_2 = 26.9, s_2 = 3.2; H_1 : \mu_1 < \mu_2, \mu_1 - \mu_2 < 0$   
 $t_0 = -3.67, t_{35,0.95} = 1.69, p = 0.0, \text{ rej. } H_0,$

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7.4.1  $H_0 : \mu_1 - \mu_2 \geq 0, \mu_d \geq 0 ; \alpha = 0.01, H_1 : \mu_1 - \mu_2 < 0, \mu_d < 0$   
 $\mu_1 - \mu_2 = d = -4, -8, -6, -1, -1, \dots n = 17, \bar{d} = -3.35294, s_d^2 = 5.117647$   
 $s_d = 2.262221; t_0 = \frac{\bar{d}}{s_d} = \frac{\bar{d}}{\frac{s_d}{\sqrt{n}}} = -6.11104, t_{16,0.99} = 2.58349; p = 0.0, \text{ rej. } H_0.$

7.4.2  $H_0 : \mu_1 - \mu_2 = 0, \mu_d = 0 ; \alpha = 0.01, H_1 : \mu_1 - \mu_2 > 0, \mu_d > 0$   
 $n = 13, \bar{d} = 5.46923, s_d^2 = 9.687$   
 $s_d = 3.11244; t_0 = 6.335725, t_{12,0.99} = 2.68; p = 0.0, \text{ rej. } H_0.$

7.4.3  $H_0 : \mu_1 - \mu_2 = 0, \mu_d = 0 ; \alpha = 0.05, H_1 : \mu_1 - \mu_2 \neq 0, \mu_d \neq 0$   
 $\mu_1 - \mu_2 = d = -9, 0, -1, -7, -7, 2, -1, -3 \quad n = 8, \bar{d} = -3.25, s_d^2 = 15.6429$   
 $s_d = 3.95511; t_0 = \frac{\bar{d}}{s_d} = \frac{\bar{d}}{\frac{s_d}{\sqrt{n}}} = -2.32418, t_{7,0.975} = 2.364; p = 0.053, \text{ do not rej. } H_0.$

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7.5.1  $\hat{p} = 0.63, H_0 : p \leq p_0 = 0.6, H_1 : p > 0.6, n = 696, \alpha = 0.05$   
 $z_0 = \frac{\hat{p} - p_0}{\sqrt{\frac{p_0(1-p_0)}{n}}} = 1.61555, z_{0.95} = 1.645, p = 0.053; \text{ do not rej.}$

$H_0$ ; not more than 60%.

7.5.2  $\hat{p} = 0.216, H_0 : p \leq p_0 = 0.15, H_1 : p > 0.15, n = 119, \alpha = 0.05$   
 $z_0 = \frac{\hat{p} - p_0}{\sqrt{\frac{p_0(1-p_0)}{n}}} = 2.01633, z_{0.95} = 1.645, p = 0.022; \text{ rej. } H_0; \text{ more}$

than 15%.

7.5.3  $\hat{p} = 0.66, H_0 : p \leq p_0 = 0.6, H_1 : p > 0.6, n = 670, \alpha = 0.05$   
 $z_0 = \frac{\hat{p} - p_0}{\sqrt{\frac{p_0(1-p_0)}{n}}} = 3.17, z_{0.95} = 1.645, p = 0.001; \text{ rej. } H_0; \text{ yes.}$

7.5.5  $\hat{p} = 0.1,$

$H_0 : p \geq p_0 = 0.15, H_1 : p < 0.15, n = 250, \alpha = 0.05$

$$z_0 = \frac{\hat{p} - p_0}{\sqrt{\frac{p_0(1-p_0)}{n}}} = -2.214, \quad z_{0.95} = 1.645, \quad p = 0.0134; \text{ rej. } H_0; \text{ yes.}$$


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7.6.1

$$n_1 = 67, x_1 = 46; n_2 = 57, x_2 = 10; \hat{p}_1 = 0.686567, \hat{p}_2 = 0.175439; \alpha = 0.01 \\ H_0 : p_1 \leq p_2, \quad H_1 : p_1 > p_2; \quad \bar{p} = \frac{56}{124} = 0.451613$$

$$z_0 = \frac{\hat{p}_1 - \hat{p}_2}{\sqrt{\frac{\bar{p}(1-\bar{p})}{n_1} + \frac{\bar{p}(1-\bar{p})}{n_2}}} = 5.699, \quad z_{0.99} = 2.326, \quad p = 0.0$$

$$7.6.4 \quad n_1 = 150, x_1 = 21; n_2 = 200, x_2 = 48; \hat{p}_1 = 0.14, \hat{p}_2 = 0.24; \alpha = 0.05$$

$$H_0 : p_1 = p_2, \quad H_1 : p_1 \neq p_2; \quad \bar{p} = \frac{69}{350} = 0.197143$$

$$z_0 = \frac{\hat{p}_1 - \hat{p}_2}{\sqrt{\frac{\bar{p}(1-\bar{p})}{n_1} + \frac{\bar{p}(1-\bar{p})}{n_2}}} = -2.32711, \quad z_{0.975} = 1.96, \quad p = 0.01$$


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