

King Saud University  
College of Engineering  
Electrical Engineering Department

EE 329

Final Exam

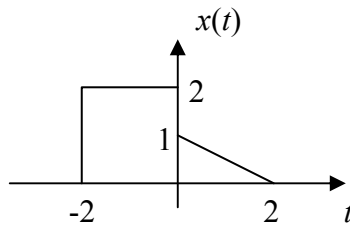
Instructor: <b>Dr. Mohammed Al Eshaikh</b>
Date: <b>27/5/1428</b>
Time: <b>8:00-11:00 am</b>

Question	Mark
1	
2	
3	
4	
5	
Total	

	اسم الطالب:
	الرقم الجامعي:
	الشعبة:

Problem 1

a) The signal  $x(t)$  is as shown



- i) Find the energy and power in the signal  $x(t)$ .
- ii) Sketch the signal  $x(2t+1)$ .
- iii) Sketch the even and odd part of  $x(t)$ .

b) Determine whether or not each of the following signals is periodic. If the signal is periodic find the fundamental period.

i)  $x_1(n) = 4 \sin\left(\frac{4\pi}{3}n - \frac{5\pi}{3}\right) + e^{j\left(\frac{3\pi}{5}n + 3\pi\right)}$

ii)  $x_2(t) = 5 \sin\left(\frac{3\pi}{2}t^2\right)$

iii)  $x_3(n) = u(n) + u(-n) - \delta(n)$

## Problem 2

Discuss the following properties of the given system:  $y(t) = 3x^2(t + 5)$

i) Memoryless ii) Causal iii) linear iv) Time invariant v) Stable. vi) Invertible.

### Problem 3

Compute and plot  $y(n) = x(n) * h(n)$ , where

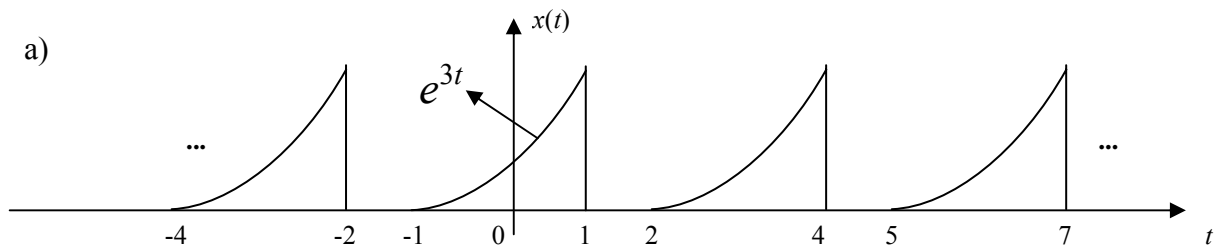
$$x(n) = u(n-2) - u(n-11)$$

$$h(n) = u(n+1) - u(n-4)$$

$$\text{(Hint: } \sum_a^b 1 = b - a + 1)$$

Problem 4

a)



For the above continuous-time periodic signal:

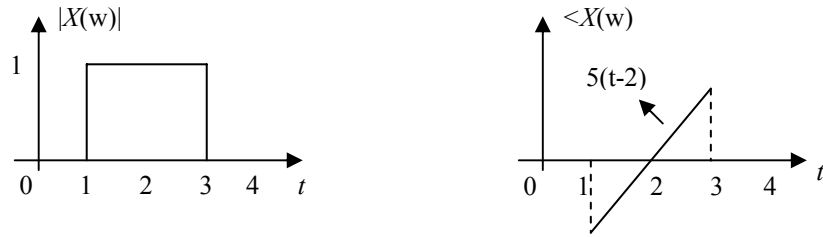
- i) Find the fundamental period and the dc component of  $x(t)$ .
- ii) Find Fourier series coefficients  $a_k$  of  $x(t)$ .

- b) A periodic signal  $x(t)$  is real valued and has a fundamental period  $T = 8/3$ . The nonzero Fourier series coefficients for  $x(t)$  are:  $a_1 = a_{-1} = 1$ ,  $a_3 = a_{-3}^* = 1 + j$   
Express  $x(t)$  in the form

$$x(t) = \sum_{k=0}^{\infty} A_k \cos(\omega_k t + \phi_k)$$

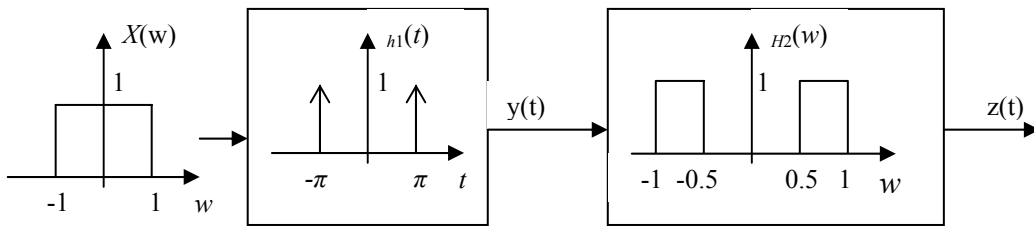
Problem 5

a)



The above Figure shows  $X(\omega)$  as magnitude and phase, use the inverse Fourier transform to find  $x(t)$ .

b)



Find and sketch  $Y(\omega)$  and  $Z(\omega)$ . (Hint:  $\delta(t) \Leftrightarrow 1$ )

c) Consider the Fourier transform pair:  $\frac{2}{1+t^2} \Leftrightarrow 2\pi e^{-|w|}$

Determine the Fourier transform of the following signals

i)  $x_1(t) = \frac{2}{1+9t^2}$       ii)  $x_2(t) = \frac{2}{1+(t+2)^2}$

iii)  $x_3(t) = \frac{6}{1+t^2} e^{j5t}$       iv)  $x_4(t) = \frac{-4t}{(1+t^2)^2}$

d) an LTI system can be described as  $\frac{d}{dt} y(t) + 3y(t) = 2x(t-1)$

i) Find the transfer function of this system

ii) Is this system stable? (Hint:  $e^{-at} u(t) \Leftrightarrow \frac{1}{a+jw}$ )